Workshop 1:

Sample Size Determination-Methodology and Philosophy



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"How many do I need ?...."

Objectives

- Not a statistics or programming course!
- Enough information to enable you to:
 - understand (critique) what you read in the medical literature.
 - "In order to have 90% power to detect a hazards ratio of 1.33 between the two treatment arms (an improvement of median survival from 6 to 8 months), using a two-sided 5% level test, a minimum of 520 deaths will be needed before the final analysis."
 - think clearly about your own research <u>before</u>, during and after data collection and identify some common
 - know what your input should be when seeking additional statistical assistance for study design / sample size.

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Statisticians are like drunks leaning against the lamp post - they are there for support, not illumination.



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Sample Size in Medical Trials

"How many subjects are needed to assure a given probability of detecting a statistically significant effect, of a given magnitude, if one truly exists?"

What is the...

- smallest effect worth detecting?
 - Clinical relevance
- acceptable risk of seeing it, if it doesn't exist?
 - Statistical significance level $\alpha,$ Type I error
- acceptable risk of missing it, if it exists?
 - Power β, Type II error (1-β)

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Experimental Errors State of Nature (Reality) No Effect Effect Type II Statistical Analysis (β) error 'Accept' null hypothesis when it is false No Effect Results of 'Accept' null hypothesis when it is true Type I (α, p) error Effect Reject null hypothesis Reject null hypothesis when it is true when it is false Dr CJ O'Callaghan

Sample Size Calculations

- Define null and alternative hypotheses
 - determine minimum difference to be detected or of interest
- Specify type I error (significance level)
- Specify type II error (power)
 - specify sample size and determine power...

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Statistical Hypotheses

- An experiment or set of observations never proved anything.
- The purpose of statistical tests, is to determine if the obtained results provide a reason to reject the *hypothesis* that they are merely a product of chance factors.

• Null Hypothesis: H₀

Alternate Hypothesis: H_A

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Induction and Deduction

White Swans

"No matter how many instances of white swans we may have observed, this does not justify the conclusion that all swans are white"

Sir Karl Popper

•A black one may be lurking just around the corner?



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Define H₀ and H_a

- H₀ is the reverse of what we hope/believe; it is put forward to allow the data to contradict it and is typically a hypothesis of no difference or no effect.
- Examples (different endpoints/objectives):
 - Comparing two means
 - H_0 : $M_1 = M_2$ VS H_a : $M_1 > M_2$ (or $M_1 \neq M_2$)
 - Comparing two proportions
 - H_0 : $P_1 = P_2$ VS H_a : $P_1 > P_2$ (or $P_1 \neq P_2$)
 - Comparing two survival functions
 - H_0 : $S_1 = S_2$ for all $t \vee S$ Ha: $S_1 > S_2$ (or $S_1 \neq S_2$) for some t

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Clinical "Significance"

- a.k.a. a clinically meaningful difference
- statistical significance is necessary but not sufficient for clinical significance
- depends on implications of detected difference (e.g. 1 week improvement in median overall survival**)
- "given a large enough sample size, you will likely detect a statistically significant difference"

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Minimum Difference to be Detected

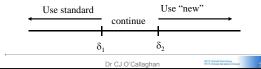
- This difference can be the difference that:
 - is likely to be present
 - would make a difference to clinical practices
- Determine minimum clinically important difference
 - Previous results
 - Pre-clinical or pilot studies
 - Clinical experiences and judgments

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Freedman et al. Formulation

- What is the minimum improvement from the new treatment which would lead you to adopt the "new" treatment as routine (δ₂)?
- What is the maximum improvement from the new treatment which would lead to your retention of the standard treatment as routine (δ₁)?



Significance Level

- In hypothesis testing, the significance level is the criterion used for rejecting the null hypothesis.
- The significance level is used in hypothesis testing as follows:
 - The difference between the results of the trial and H₀ is determined.
 - Assuming H₀ is true, the probability of a difference that large or larger is computed.
 - This probability (p) is compared to the significance level (α). If p≤ α, then H₀ is rejected and the outcome is said to be statistically significant.

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Significance Level

- •Traditionally, either the 0.05 level (sometimes called the 5% level) or the 0.01 level (1% level) have been used, although the choice of levels is largely subjective.
- •The lower the significance level, the more the data must diverge from the null hypothesis to be significant. Therefore, the 0.01 level is more conservative than the 0.05 level... but not a linear relationship.

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An Aside: Probability Value

- In hypothesis testing, the probability value (sometimes called the p value) is the probability of obtaining a statistic as different from or more different from the parameter specified in H₀ as the statistic obtained in the experiment.
- The significance level (α)is an arbitrary threshold for comparison / decision

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p < 0.05

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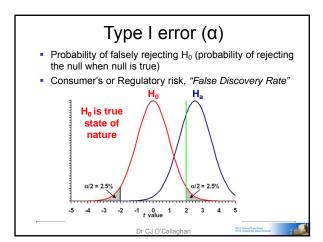
p = 0.49

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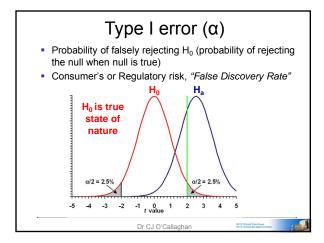
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p =	= 0.0	59
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Aside: Sampling Distribution a sampling distribution is the probability distribution of a given statistic based on a random sample of certain size n. It may be considered as the distribution of the statistic for all possible samples of a given size. The sampling distribution depends on the underlying distribution of the population, the statistic being considered, and the sample size used.



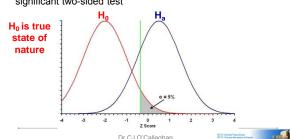
1-sided vs 2-sided Alternatives

- Use one-sided test if you "know" the experimental arm is better than the standard arm (then why do you need a RCT?) or you are only interested in this type of question
- ...but if the null hypothesis is not rejected, it cannot tell whether experiment arm is worse than the standard arm
- FDA's position is two-sided alternatives for almost all studies
- For hypothesis generation, a two-sided test should be used

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One-sided a

- "Lowers the bar" for the same apparent degree of risk
- Implies knowledge which may not necessarily be assumed
- Cheating? a one-sided test could make 'significant' a non-significant two-sided test



Corollary: Accepting the Null Hypothesis?

- A null hypothesis is not accepted just because it is not rejected.
- Data not sufficient to show convincingly that a difference between arms of a trial is not zero do not prove that the difference is zero.
- Such data may even suggest that the null hypothesis is false but not be strong enough to make a convincing case, for example if the probability value were p=0.08
- H₀ may or may not be true, there just is not strong enough evidence to reject it
- so called "trending toward significance", a.k.a. "pilot study"

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Minimum difference to be detected

- A negative result (i.e., when the null hypothesis is not rejected by the data) does not indicate the two arms are the same
- It only means that the actual difference is less than what we intended to detect and our sample size is not large enough to detect this difference
- A study should have enough <u>power</u> to detect a minimum difference which is clinically important

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Power, Type II error (β)

- Traditionally, power is fixed a priori, usually at 0.80 (1-β) with the chance of a Type II error (β) at 0.20
- Few studies are powered greater than 90% but MANY have lower power
- Affects the credibility of "negative" studies
 - Medical versus Ecological implications

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On Power:

- Here are the results of our drug testing study on rabbits:
- 1/3 of the sample died
- 1/3 of the sample survived
- the other one got away

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"To call in the statistician after the experiment is done may be no more than asking him to perform a postmortem examination: he may be able to say what the experiment died of."

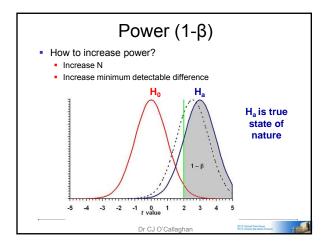
Sir R.A Fisher

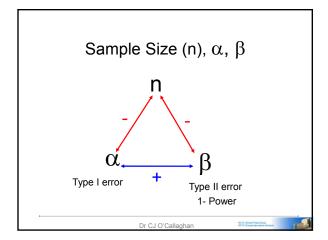
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Type II error (β) Probability of falsely accepting H₀ (probability of failing to reject H₀ given that H_a is true) Sponsor's or investigator's risk H₀ H_a is true state of nature

Power (1-β) Probability of correctly reject H₀ (probability of rejecting the H₀ given that H_a is true) Power=1-type II error H₀ H_a is true state of nature





Calculating a Sample Size

- The most difficult and important aspect of "sizing" a study is not the mathematics of sample size calculation
- it's deciding what the really relevant outcome measure is and what difference in that measure the trial will be designed to detect.

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Sample Size Description for a Difference in Times to Events

In order to have 80% power to detect a hazard ratio of 1.28 (i.e. an improvement of 4% disease-free survival from 80% at 4 years) using a two sided 5% level test, the maximum number of recurrences we would need to observe is 523. Assuming we could enter 2380 patients in 2 years, we would need to follow all patients for about 4 years before the final analysis. The maximum total duration of the trial would be 6 years. If the risk of relapse for the control group is much lower, with 2380 patients entered in two years followed for an additional four years, we would have 80% power to detect a hazard ratio of 1.5 (i.e. an improvement of 2.6% disease free survival from 92% at four years).

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Sample size for time to an event outcome

- Assume independent and exponential life times with hazard rates λ_c and λ_e for control and experimental groups respectively
- H_0 : $S_e(t) = S_c(t)$ vs H_a : $S_e(t) \neq S_c(t)$
- Since exponential times have constant hazard rates, the above hypotheses can be written as hypotheses for the hazards ratio of Δ = λ_c / λ_e .



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Number of events (d) required

 Assume all the patients will have an event at the time of final analysis. We can determine number of events (per group) required:

$$H_0: \Delta = 1 \text{ vs } H_a: \Delta = \frac{\lambda_c}{\lambda_a} \neq 1$$

$$d = \frac{2(z_{\alpha/2} + z_{1-\beta})^2}{(\ln \Delta)^2}$$

 Since there will be patients censored at the time of final analysis, we have to enter more patients and follow them for some time in order to observe the given number of events

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Total Size & Duration

- Patients are recruited over an interval θ to T_θ and then follow to the end of the study period T
- The required sample size for the study is *N*:

$$N = \frac{\left(Z_{\alpha/2} + Z_{\beta}\right)^{2} \left[\phi(\lambda_{c}Q_{c})^{-1} + \phi(\lambda_{e}Q_{e})^{-1}\right]}{\left(\lambda_{c} - \lambda_{e}\right)^{2}}$$

$$where Q_{c} = \frac{n_{c}}{N}, Q_{e} = \frac{n_{e}}{N}$$

$$\phi(\lambda) = \frac{\lambda^{2}}{1 - \left[e^{-\lambda(T - T_{0})} - e^{-\lambda T}\right]/\lambda T_{0}}$$

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Example

- H_0 : $S_e(t) = S_c(t)$ vs H_a : $S_e(t) \neq S_c(t)$
- M_e and M_c are median survivals of the experimental and control arms respectively

M _e	M _c	⊿	D=2*d	$T = T_O(N)$		
α=0.05, 1-β=0.8						
1.5	1	1.5	191	3.0 (300)		
2.0	1	2.0	65	1.5 (143)		
2.5	2	1.25	631	8.0 (910)		
3.0	2	1.5	191	4.0 (370)		
4.0	2	2.0	65	2.5 (160)		

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Help is at hand! Southwest Oncology Group A National Chief Present Oxigo Select type of Calculate Program to Calculate Prover or Sample Size Prover Sample Size Hazard rates Survival props Stata 1 Change types or strata Change types or strata Stratam proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, standard hazard ratio hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time Stratum Proportion hazard rate, expt proportion surviving Survival time

Practicum & Examples

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A PHASE III RANDOMIZED STUDY OF YTTRIUM-90 GLASS MICROSPHERES PLUS BEST SUPPORTIVE CARE VERSUS BEST SUPPORTIVE CARE ALONE IN PATIENTS WITH PRETREATED LIVER-DOMINANT METASTATIC COLORECTAL CARCINOMA

- Primary Outcome = Overall Survival
- 1:1 Randomization (2:1?)
- Alpha = 0.05, 2-sided (1-sided?)
- Power = 90% (80%?)
- Accrual Rate = 100 patients per year (150?)
- Duration of Follow-up = 12 months (6 months?)
- Median Survival in Control Arm = 4.6 months (6 months?)
- Hazard Ratio to Detect = 1.43 (1.36?)
 - (6.6 months to 4.6 months ... or ... 8.6 months to 6 months)
 - (6.3 months to 4.6 months ... or ... 7.7 months to 6 months)

Sample Size?

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• Primary Outcome = OS Primary Outcome = OS 2:1 Randomization ↑ 1:1 Randomization ■ Alpha = 0.05, 1-sided ↓ Alpha = 0.05, 2-sided • Power = 80% ↓ Power = 90% ■ Accrual Rate = 150 / year ↓ Accrual Rate = 100 / year Duration of Follow-up = 12 months Duration of Follow-up = 6 months Median BSC Survival = 4.6 months • Median BSC Survival = 6 months ■ Hazard Ratio to Detect = 1.36 ↑ Hazard Ratio to Detect = 1.43 = 350 = 356 Accrued over 2.3 years Accrued over 3.6 years Total duration = 2.8 years Total duration = 4.6 years

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